# Commutative Diagrams with $X_{Y}$-pic I. Kernel Functions and Arrows 

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Abstract This the first of two papers aiming to describe the use of the facilities of the package $X_{Y}$-pic for constructing commutative diagrams. We tried to use in a systematic way the "learning by examples" approach, without entering into the details of different constructions or trying to describe in an exhaustive way all the possibilities. The final goal is to provide the reader with enough knowledge to be able to construct by himself complicated diagrams. This first paper describes the basic possibilities of $X_{Y}$-pic, which are provided by the kernel of the associated language, but it also explores many of the opportunities provided by the extension arrow.

## 1 Introduction

Commutative diagrams lie at the very heart of mathematics and, therefore, it is very fortunate that both $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ and $\mathrm{IAT}_{\mathrm{E}} \mathrm{X}$ provide ways of construction for such objects. There are many packages devoted entirely or partially to such a purpose. Usually, they work both under plain $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ and $\mathrm{LAT}_{\mathrm{E}} \mathrm{X}$, with minimal modifications. Most of them are examined and compared by G. Valiente Feruglio [8] in an old issue of TUGboat.

Unfortunately, the general purpose introductions to $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ or $\mathrm{IAT}_{\mathrm{E}} \mathrm{X}$ typically ignore commutative diagrams, with the notable exception of the amslatex package amscd, which is very easy to use but, unfortunately, allows only vertical and horizontal arrows. For the rest, the user is either left at the mercy of the original documentation accompanying the package (which is not always very complete,
let alone pedagogical) or is required to consult more specialized books, such as The ${ }^{L A T} T_{E} X$ Graphics Companion [3], which are not always available.

This is the first of two articles aiming to describe the commutative diagrams capabilities of one of the most complex packages, $X_{Y}$-pic. This package, written both for plain $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ and $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$, is quite ambitious and offers possibilities of drawing a lot more things than just commutative diagrams. We only intend, however, to describe the main tools for constructing such diagrams, either by using the primitive elements of the graphics language of $X_{Y}$-pic (what we call the kernel of $X_{Y} Y$-pic), or by using more advanced constructions and environments. We ought to mention that, in fact, the package was created, originally, by Kristoffer Rose, exactly for "typesetting pretty diagram arrows with $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ " (see [4]).

In this article we will discuss the basic possibilities of $X_{Y}$-pic, namely, essentially, constructing diagrams by assigning coordinates to different objects and connecting these objects with different kinds of arrows. In the second article we shall describe:

- the frame extension, allowing one to put frames (of several shapes) around objects;
- the xymatrix environment (enclosed in the matrix extension), allowing the representation of the diagrams as arrays (matrices) of objects, providing an easier and more straightforward way of constructing diagrams, without using coordinates to identify the position (but, also, losing some of the flexibility);
- the 2 cell extension, devoted to the construction of a special class of diagrams, very common in the theory of categories;
- several other fine points of the program.

This article is largely based on the original documentation of the "founding fathers" K. Rose and R. Moore, the reference manual [6] and user's guide [5], but also on a recent, excellent tutorial (in Portuguese) by Carlos Campani [1] and the chapter on $X_{Y}$-pic from The $L^{A} T_{E} X$ Graphics Companion [3].

## 2 How XY-pic works

$X_{Y}$-picisapackagedesignedtobeusedbothforPlain$\mathrm{T}_{\mathrm{E}}X$and$\mathrm{LAT}_{\mathrm{E}}X$.Therefore,inthetreeofany$\mathrm{T}_{\mathrm{E}}\mathrm{X}$distribution,itliesinthegenericsectionofthetexmftree.IfusedbyPlain$T_{E}X$,itisloaded,asusual,bythecommand\inputxyatthebeginningofthefile.Ifitisusedina$\mathrm{LAT}_{\mathrm{E}}\mathrm{X}$document,thenitisloadedbyacommand\usepackage[options]\{xy\}used,ofcourse,inthepreambleofthedocument.Theoptionssimplymeans,inmostcases,theactivationofsomeoftheextensions.Ifyouarenotsurewhetheranextensionhastobeactivatedornot,youcanplayitsafeandactivatealltheextensions,bytheoptionall.Wemention,however,thatthereareoptionswhicharenotenclosedinthisallandwhichhavetobeprescribedindependently.Seethereferencemanualfordetails.undefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefined

In Plain $T_{E} X$ you can activate an option by the command
\xyoption\{option\}
With a single notable extension, which will be described bellow (the \txt construction), all $X_{Y}$-pic constructions should be enclosed in an environment, call xy. For this environment, two syntaxes are provided:

- a Plain $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ version: \xy . . \endxy
- a $\operatorname{LAT}_{\mathrm{E}} X$ version: \begin\{xy\} . . } \backslash end \{ x y \} .

In a ${ }^{L A} T_{E} X$ document you can use whichever syntax you like, in Plain $T_{E} X$ however, only the first one is accepted. We shall use, throughout this document, exclusively the $\mathrm{AT}_{\mathrm{E}} \mathrm{X}$ syntax, so, if you want to use any of the examples in a $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ document, all you have to do is to switch to the other syntax of the xy environment.

Working with $X_{Y}$-pic is very much like programming with an object-oriented programming language. In fact, the authors of the $X_{Y}$-pic system devised a (quite complicated) language (the previously mentioned kernel of the system) with which one can make very complex drawings. It is by no means the aim of this
paper to describe the details of this language. For this, the reader may consult the reference manual. The philosophy of the system, however, is quite easy to explain. For our needs, at least, the following elements of the kernel are crucial:
positions - they are nothing but the pair of coordinates of a point of the figure. The coordinate system is local: it is related to each figure, not to the page.
objects - they are thought of as boxes that, unlike ordinary $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ boxes, have edges. They can be circular, elliptic or rectangular and there is an entire set of operations that can applied to them. We shall discuss more about objects in the sequel of this paper. For now, an object will be, for us, just an ordinary "box" containing one or more $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ symbols.
directionals - they provide ways of connecting different positions and can be of two kinds:

1. connectors - they are used to construct the shaft (the body) of the arrow;
2. tips - they are used to construct the tail and the head of the arrow.
decorations - other things that are added to the diagram (e.g., labels).
Thus, to construct a diagram with $X_{Y}$-pic, you have to use the following steps:
3. choose the positions (the coordinates) of the vertices of the diagram;
4. drop some objects at these positions (these objects will be the origins and targets of the arrows);
5. connect the positions with arrows;
6. add whatever extra information you want (e.g. labels or text).

Apart from the basic elements of the $X_{Y}$-pic, which was described, roughly, above, the system also includes some extra goodies, which are called options. They are, somehow arbitrary, divided into two classes:

1. extensions - they add some more objects and methods. Typical for this kind of enhancement of the kernel are the extension frame, which will be described in the second article and which offer the possibility of "framing" the objects, and the extension curve, which we will use in this paper to construct curved arrows.
2. features - they provide notations for particular applications areas. In this class fall the options: arrow, matrix, polygons, lattices, knots, 2cell.

We mention, in the end of this short description, that everything that happens inside an xy environment is in mathematical mode. If you want to drop somewhere ordinary text, there is provided a special command for that. Nevertheless, if you want your diagrams to be numbered, you can include them into an equation environment.

## 3 Basic constructions

### 3.1 Constructing arrows from pieces

The simplest operation we can make with $X_{Y}$-pic is, probably, dropping an object on a position. It is made with the operator $*\}$ :

A

$$
\begin{aligned}
& \backslash \text { begin }\{x y\} \\
& (0,0) *\{A\} \\
& \backslash e n d\{x y\}
\end{aligned}
$$

We defined a position of coordinates $(0,0)$ and we attached to this position the label $A$. To construct diagrams, we should also be able to draw line connecting the vertices of the diagram. This is done in $X_{Y}$-pic with the so-called directionals, "employed" by the operator **. The directionals are of two species:

1. connectors - they construct the connecting line itself (the shaft of the arrow) (see table 1 for a list of most frequent connectors);
2. tips - they construct the head or the tail of the arrow (see table 2).

Of course, the tips may be absent. The simplest example is the following:
$A-B$

$$
\begin{aligned}
& \text { \begin } \{ \mathrm { xy } \} } \\
{(0,0) *+\{\mathrm{A}\} ; \quad(10,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\}} \\
{\text { \end\{xy } }
\end{array}
\end{aligned}
$$

In this situation, we used a single connector. $\backslash \operatorname{dir}\{-\}$ connects the two positions with a single solid line. Notice the two + signs after the $*$ 's. They introduce


Table 1: Directionals (connectors)


Table 2: Directionals (tips)
some extra space around the labels, otherwise the connection line would be too close to them. Notice, also, that we have to add a semicolon ; before any new position is defined. The connector provides a link between the last two positions we defined. Adding a head or a tail (or both) to a line to produce an arrow is slightly more complicated. The syntax for the command producing a tip is identical to the one of the connector, only the argument is of a different kind, e.g. \dir\{>\}. We might be tempted to think that it is enough to add a command of this kind to the above example. The result looks like in the figure bellow and it indicates that the system interprets this command as a connector, also:

```
>>>
```

```
\begin\{xy\} }
```

\begin\{xy\} }
$(0,0) *+\{\mathrm{A}\} ;(10,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\}$
$(0,0) *+\{\mathrm{A}\} ;(10,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\}$
**\dir\{>\}
**\dir\{>\}
\end\{xy\} }

```
\end\{xy\} }
```

What we have to do is to use another operator, ?, to indicate, first, where the tip should be added. The full syntax is ?>*, if we want to add the tip at the end (i.e. near last defined position), or ?<* if we want to add the tip at the origin. We have, thus:

```
A\longrightarrowB
\begin{xy}
(0,0)*+{A}; (10,0)*+{B} **\dir{-}
    ?>* \dir{>}
\end{xy}
or,
\(A \leftarrow B\)
```

```
\begin{xy}
```

$$
\begin{xy}
(0,0)*+{A}; (10,0)*+{B} **\dir{-}%
(0,0)*+{A}; (10,0)*+{B} **\dir{-}%
    ?<* \dir{<}
    ?<* \dir{<}
\end{xy}
$$

```
\end{xy}
```

or, if we want to add tips at both sides,

$$
\begin{array}{ll}
A \leftrightarrow B \quad & \text { lbegin }\{\mathrm{xy}\} \\
& (0,0) *+\{\mathrm{A}\} ;(10,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\} \% \\
& ?>* \backslash \operatorname{dir}\{>\} ?<* \backslash \operatorname{dir}\{<\} \\
& \text { lend }\{\mathrm{xy}\}
\end{array}
$$

If we use several < or > signs between ? and $*$, then we can put the tip also at an intermediate position:
$A<B$

```
\begin{xy}
(0,0)*+{A}; (10,0)*+{B} **\dir{-} ?<<<<* %
\dir{<}
\end{xy}
```

We can do this, also,

$$
A<B
$$

```
\(\backslash\) begin \(\{x y\}\)
\((0,0) *+\{\mathrm{A}\} ;(10,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\} \quad ?(.5) * \%\)
    \dir\{<\}
\end\{xy\} }
```

Of course, we can add different kind of tips:

```
A\bulletB
```

```
\(\backslash\) begin \(\{x y\}\)
```

$\backslash$ begin $\{x y\}$
$(0,0) *+\{\mathrm{A}\} ;(10,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\} \%$
$(0,0) *+\{\mathrm{A}\} ;(10,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\} \%$
?>* \dir\{>\} ?<* \dir\{*\}
?>* \dir\{>\} ?<* \dir\{*\}
\end\{xy\} }

```
\end\{xy\} }
```


### 3.2 Commands for arrows

To simplify the syntax for directionals, which has the tendency of becoming quite complicated, $X_{Y}$-pic also provides "composite" directionals, i.e. arrows. To use them, you have to activate the option arrow. For instance, to draw an arrow from a position to another, we have to use something like


Table 3: Arrows

\begin } \{ \mathrm { xy } \} $\\{\{\backslash \operatorname{ar}(0,0) *+\{\mathrm{A}\} ;(10,10) *+\{\mathrm{B}\}\}} \\{\backslash \operatorname{end}\{\mathrm{xy}\}} \end{array}$
\ar is the simplest notation for an arrow. The complete syntax is of the form \ar@\{type\}, (see the table 3). \ar is a shorthand for \ar@\{->\}. The table 3 contains some of the most commonly used arrows. We have to mention, however that $X^{\prime}{ }^{-}$ pic actually offers the possibility of constructing a lot more arrows, by using one of the following commands:

1. \ar@variant\{tail shaft head\}
2. $\backslash$ ar@\{head $\}$
The head and the tail (i.e. the tips) can be any of the combinations from the table 4. In the table they are shown as heads of arrows, but they can be used, equally, as tails.

The shafts of the arrows can be any of the arguments of the \dir command from the first column of the table 1. As for the variant, they either indicate how the tip should be positioned ("above" or "below"), either that the shaft should be doubled or tripled. More specifically, the four available variants are:


Table 4: Arrow tips

  -       - the "above" variant. You should experiment with it. The action depends on the tip. It either indicates that the tip should be placed eccentrically ("above", with the convention that this means, actually, on the left, when we look at the arrow from tail to head), either that we should use only the upper part of the tip. See the examples below.
_ - the "below" variant. The same remarks as above are in order, if we substitute "above" with "below" and "left" with "right".
2 - the "double" variant. The effect is that the shaft is doubled. See examples below.

3 - the "triple" variant. The effect is, of course, that the shaft is tripled.
The examples bellow show how the four variant work for the selection <-> of the triple tail-shaft-head:

$$
\begin{aligned}
& @\{\langle->\} \quad A \longleftrightarrow B \\
& \mathfrak{Q}^{\wedge}\{<->\} \quad A \longrightarrow B \\
& @_{-}\{<->\} \quad A=B \\
& \text { @ } 2\{<->\} \quad A \Longleftrightarrow B \\
& \text { @3\{<->\} } \quad A \Longleftarrow B
\end{aligned}
$$

These kind of variants work well with the kind of head and tail from the example above. In other situation, however, we might want to "raise" or "lower" only the head or the tail, not both. Fortunately, this is also possible, because we can have access to each of the component of the arrow and we can apply the chosen variant to each. By doing so, we can produce, for instance, "monsters" like


```
\begin{xy}
{\ar@{^{(}2{-}_{>}} (0,0)*+{A}; (20,0)*+{B}}
\end{xy}
```

as well as perfectly normal and very useful arrows as


```
\begin{xy}
{\ar@{~{(}->} (0,0)*+{A}; (20,0)*+{B}}%
{\ar@{_{(}->} (0,-5)*+{C}; (20,-5)*+{D}}%
{\ar@{|-_{>}} (0,-10)*+{E}; (20, -10)*+{F}}
\end{xy}
```

From the way our "monster" looks like, we can draw one conclusion: although it is, technically, possible to use a variant only for the shaft, or for the shaft and one or both of the tips, in practice this possibility is useless, because the corresponding tips are not enlarged to encompass a double or a triple of the shaft.

Let us mention, finally, that it is possible to indicate only the head of the arrow and, in this case, the program produces an arrow without tail and with the standard shaft:


```
\(\backslash\) begin\{xy\}
\(\{\backslash \operatorname{ar} @\{>\}(0,0) *+\{\mathrm{A}\} ;(20,0) *+\{\mathrm{B}\}\}\)
\end\{xy\} }
```

See the reference manual or the user's guide for even more possibilities.

### 3.3 Curved arrows

Sometimes we have to use curved arrows, for different reasons (for instance, to avoid a large label or for connecting two distant vertices of the diagram). It is possible to do that with $X_{Y}$-pic in a very simple manner. Beware, first of all, that the option curve has to be active. The syntax of the command is \ar@\{type\}@/_length/ or \ar@\{type\}@/^length/, depending on which part we want the curving to take place. Here, the length can be expressed in any accepted $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ unit.

```
A\longrightarrowB
```

```
\begin{xy}
```

$$
\begin{xy}
{\ar@{=}@/_{1pc}/ (0,0)*+{A}; (15,0)*+{B}}
{\ar@{=}@/_{1pc}/ (0,0)*+{A}; (15,0)*+{B}}
\end{xy}
$$

```
\end{xy}
```

It is even possible to omit the length and then the program will curve the arrow by a default quantity:

```
A\longrightarrowB
```

```
\begin{xy}
{\ar@{->}@/~/ (0,0)*+{A}; (15,0)*+{B}}
\end{xy}
```


### 3.4 Labelling arrows

Putting a label on an arrow is not difficult. There are more ways of doing it. If you construct the arrow by indicating separately the body and the tips, then you can add a label in the following way:


```
\begin{xy}
(0,0)*+{A}; (20,0)*+{会} **\dir{-}%
?>*\dir{>} ?*!/_2mm/{\alpha}
\end{xy}
```

The core of the label is ? $*\{\backslash$ alpha\}. If we would use only that, the label would stay on the arrow. The part !/_ $2 \mathrm{~mm} /$ represent a shift. Don't get confused: in $X_{Y}-$ pic the underscore _ indicates that the label is on the left of the arrow (when looking from tail to head), while the sign ~ indicates that the label should be on the right. By default, labels are on the left. If, in the previous example, we omit the part /_2mm/, keeping the exclamation mark, we get


```
\begin\{xy\} }
\((0,0) *+\{\mathrm{A}\} ;(20,0) *+\{\mathrm{B}\} * * \backslash \operatorname{dir}\{-\} \%\)
?>*\dir\{>\} ?*!\{\alpha\}
\end\{xy\} }
```

If we draw an arrow by using a specific command, then we have two opportunities to add labels:


```
\begin{xy}
{\ar (0,0)*+{A}; (20,0)*+{B}}%
    ?*!/_2mm/{\alpha}
\end{xy}
```

which means that the label command has exactly the same syntax and it is placed immediately after the arrow was produced. A second possibility is:


```
\begin{xy}
{\ar^{\alpha} (0,0)*+{A}; (20,0)*+{B}}%
\end{xy}
```

Notice two things:
    - this time the label is on the left, although we used the exponentiation sign;
    - the label is smaller.

The reason is that, in this case, the label is thought of as an exponent (or an index, if we use the underscore).

Also, in this case, we have an extra possibility, allowing us to put the label on the arrow, which is interrupted, to accommodate the label:

## $A \longrightarrow \alpha \longrightarrow B$

```
\begin{xy}
{\ar |{\alpha} (0,0)*+{A}; (20,0)*+{B}}%
\end{xy}
```

Implicitly, the label is placed on the middle. Be careful, though, is not necessary the middle of the arrow, is the middle of the entire construction (objects + arrow):


```
\begin{xy}
{\ar^{\alpha} (0,0)*+{A\otimes C};%
    (20,0)*+{B}}%
\end{xy}
```

Therefore, in many situations, you will have to position the label explicitly by yourself. This is easy to do, no matter which of the two syntaxes you use.

If you want to put the label at one of the two ends of the arrow, just add a < (for the tail) or a > (for the head), at the right position, meaning, if you use the command starting with a ? - immediately after the question mark. If you use the other command, then put these signs immediately after the signs ", _ or I, whichever is used.

Here are some examples:


```
\begin{xy}
{\ar (0,0)*+{A}; (20,0)*+{B}}%
    ?>*!/_2mm/{\alpha}
\end{xy}
```


$\backslash$ begin $\{x y\}$
$\left\{\backslash \mathrm{ar}^{\wedge}<\{\backslash \mathrm{alpha}\}(0,0) *+\{\mathrm{A}\} ;(20,0) *+\{\mathrm{B}\}\right\} \%$
\end\{xy\} }

If you put several > or < signs in a row, the label will move away from the corresponding end of the diagram:
$A \xrightarrow{a} B$
$$
\begin{xy}
\begin{xy}
{\ar^<<<<{\alpha} (0,0)*+{A};%
{\ar^<<<<{\alpha} (0,0)*+{A};%
    (20,0)*+{B}}
    (20,0)*+{B}}
\end{xy}
\end{xy}
$$

A simpler way of doing that is to use, instead of the characters < and >, a single decimal number between 0 and 1.0 is equivalent to $<$ and 1 is equivalent to $>$, while 0.5 will correspond, again, to the middle of the construction (not the middle of the arrow, unless the source and the destination of the arrow have equal width):
$A \xrightarrow{\alpha} B \otimes_{R} C$

```
\begin{xy}
{\ar^(.4){\alpha} (0,0)*+{A};%
    (20,0)*+{B\otimes_{R}C}}%
\end{xy}
```

If you want to put the label in the middle of the arrow, when the two vertices are not of the same size, you can do that by adding a minus sign before the label, as in the following example:

$$
A \xrightarrow{\alpha} B \otimes_{R} C \quad \begin{array}{ll} 
& \text { begin }\{\text { xy }\} \\
& \{\backslash \text { ar } \\
& (20,0) *+\{B \backslash \text { alphatimes_ }\{\mathrm{R}\} \mathrm{C}\}\} \% \\
& \text { lend }\{\mathrm{xy}\}
\end{array}
$$

You can put more then one label on the same arrow (why would anyone want to do this?!):

$$
A \xrightarrow[\beta]{\alpha} B \quad \begin{aligned}
& \\
& \\
& \left\{\text { begin }^{\wedge}\{\mathrm{xy}\}\right. \\
& (0,0) *+\{\mathrm{A}\} ;(20,0) *+\{\mathrm{B}\}\} \\
& \\
& \backslash \text { end }\{\mathrm{xy}\}
\end{aligned}
$$

You may want to use both commands for producing arrows in the same diagram:

$\backslash$ begin\{xy\}
$\backslash$ begin\{xy\}
$\{\backslash$ ar@ $/ \sim .75 \mathrm{pc} /(0,0) *+\{\mathrm{A}\} ;(20,0) *+\{\mathrm{B}\}\} \%$
$\{\backslash$ ar@ $/ \sim .75 \mathrm{pc} /(0,0) *+\{\mathrm{A}\} ;(20,0) *+\{\mathrm{B}\}\} \%$
?*!/_2mm/\{\alpha\};\%
?*!/_2mm/\{\alpha\};\%
$\{\backslash$ ar@/_. $75 \mathrm{pc} / \mid\{\backslash$ alpha\} $(0,0) *+\{\mathrm{A}\} ; \%$
$\{\backslash$ ar@/_. $75 \mathrm{pc} / \mid\{\backslash$ alpha\} $(0,0) *+\{\mathrm{A}\} ; \%$
$(20,0) *+\{B\}\}$
$(20,0) *+\{B\}\}$
\end\{xy\} }
\end\{xy\} }

There is, though, a small problem: the fonts used for the two arrows have different sizes. It is not difficult to deal with this problem. You have to choose, first, which is the size you prefer. If you prefer the larger size, just substitute, in the "inner" label, \{ \alpha\} by \{\displaystyle \alpha\}:

$$
\begin{xy}
\begin{xy}
{\ar@/~.75pc/(0,0)*+{A}; (20,0)*+{B}}%
{\ar@/~.75pc/(0,0)*+{A}; (20,0)*+{B}}%
?*!/_2mm/{\alpha};
?*!/_2mm/{\alpha};
%
%
{\ar@/_.75pc/|{\displaystyle \alpha}%
{\ar@/_.75pc/|{\displaystyle \alpha}%
    (0,0)*+{A}; (20,0)*+{B}}
    (0,0)*+{A}; (20,0)*+{B}}
\end{xy}
\end{xy}
$$
otherwise substitute in the "outer" label \{\alpha\} by\{\scriptstyle \alpha\}:


```
\begin{xy}
{\ar@/~.75pc/(0,0)*+{A}; (20,0)*+{B}}%
    ?*!/_2mm/{\scriptstyle \alpha};%
{\ar@/_.75pc/|{\alpha} (0,0)*+{A};%
    (20,0)*+{B}}
\end{xy}
```


### 3.5 Drawing multiple arrows

To draw several arrows between the same position, all we have to do is to shift them a little bit. This is done with the command @<dimension>. If the arrows have opposite directions, then the shifting can be made with the same (positive) quantity:
$A<{ }_{<} B$
$$
\begin{xy}
\begin{xy}
(0,20)*+{A}="a"; (20,20)*+{B}="b";%
(0,20)*+{A}="a"; (20,20)*+{B}="b";%
{\ar@<1.ex>"a";"b"};%
{\ar@<1.ex>"a";"b"};%
    {\ar@<1.ex> "b";"a"};
    {\ar@<1.ex> "b";"a"};
\end{xy}
\end{xy}
$$
otherwise one of them should be shifted with a negative quantity:

$$
A \longrightarrow B \quad \begin{aligned}
& \backslash \text { begin }\{x y\} \\
& (0,20) *+\{A\}=" a " ;(20,20) *+\{\mathrm{B}\}=" \mathrm{~b} " ; \% \\
& \{\backslash \operatorname{ar@<1.ex>"a";"b"\} ;\% } \\
& \{\backslash \operatorname{ar@<-1.ex>} " \mathrm{a} " ; " \mathrm{~b} "\} ; \\
& \backslash \text { end }\{\mathrm{xy}\}
\end{aligned}
$$

We can even produce curved arrows:


```
\begin{xy}
(0,20)*+{A}="a"; (20,20)*+{B}="b";%
{\ar@<1.ex>@/~.5pc/|{f}"a";"b"};%
    {\ar@<1.ex>@/_.5pc/|{g} "b";"a"};
\end{xy}
```


### 3.6 Adding text to the diagrams

Ordinary text is added in a diagram through the command
\txt<width>style\{text string\}
The text is typeset in centered paragraph mode, i.e. the line breaks can be controlled through the command $\backslash \backslash$. Here width represents the the width of the paragraph box, while style represents the style in which the text should be typeset, as the following example suggests:
$A \longrightarrow A$
This is an arrow

```
\newcommand{\smit}{\small\itshape}
\begin{xy}
{\ar (0,0)*+{A}; (25,0)*+{A}};
%
(12.5,-10)*+{\txt<4cm>\smit{This is an arrow}}
\end{xy}
```

As you can see from the example, the text can be dropped as any other object. One or both of the options for \txt can be absent. As we stated earlier, \txt works outside the $\backslash x y$ environment, but it is not really useful, because, in fact, you want to put the text in a certain position, which is only possible if you use the command inside the environment.

## 4 Drawing more complicated diagrams

The sequential way of constructing a diagram is not very efficient. It would be nice to have the possibility to draw arrows from a position to any of the already defined positions, not only to the next one or to the previous one. Fortunately, this is possible. The trick is to give names to different positions and then address them by their names, like in the following example:


```
\begin{xy}
(0,20)*+{A}="a"; (20,20)*+{亘}="b";%
(0,0)*+{C}="c"; (20,0)*+{D}="d";%
{\ar "a";"b"}?*!/_2mm/{\alpha};
{\ar "a";"c"};{\ar "b";"d"};%
{\ar "c";"d"};%
{\ar@{-->} "a";"d"};?*!/_2mm/{\gamma};
\end{xy}
```

As one can see very easily, we assigned to each position a name (don't forget the quotation marks!), and then we used the names to define arrows from a position to another.

To draw "spatial" diagrams, we need an opportunity to suggest the spatial character, by interrupting some of the arrows. $X_{Y}$-pic provides such an opportunity, as well.


```
\begin{xy}
(0,20)*+{A}="a"; (20,20)*+{亘}="b";%
(0,0)*+{C}="c"; (20,0)*+{D}="d";%
{\ar@{->} "a";"d"};
{\ar@{->}|>>>>>>>>>>>>{\hole} "b";"c"}
\end{xy}
```

What we are doing is to insert a hole in one of the arrows, at the "right place". With the command |>>... (put as many > sign as it takes), you just fix this position. This is done by trial and error. Again, it is possible also to use several < signs to indicate the distance from the other end or, even simpler, substitute these signs
with a fractional decimal number between parentheses, as we explained when we talked about labels.

Here follows a first example of more complicated diagram (adapted from the user's manual), in which are applied several of the constructions described so far. These kind of diagrams are common in the theory of categories, especially when one wishes to describe universality properties.


```
\begin{xy}
(0,40)*+{U}="u"; (30,20)*+{X\times_ZY}=%
"xzy";%
(55,20)*+{X}="x";(30,-5)*+{Y}="y";%
(55,-5)*+{Z}="z";%
{\ar@{->}_p "xzy";"x"};%
    {\ar@{->}^q "xzy";"y"};%
        {\ar@{->}^g "y";"z"};
{\ar@{->}^f "x";"z"};%
{\ar@{->}|{(x,y)}"u";"xzy"};%
{\ar@{->}@/~0.5pc/^x "u";"x"};%
{\ar@{->}@/_/_{y} "u";"y"};
\end{xy}
```


## 5 Complex diagrams from real life

In this final section of the article we shall construct several complex diagrams taken from books of the theory of categories or algebraic topology, to illustrate the power of $X_{Y}$-pic.

The following diagram (taken from the book of categories theory by Horst

Schubert (vol. I, p. 135)

was produced by the following code:

```
\begin{xy}
%vertices
(15,30)*+{\bigsqcup M_e}="v1";(45,30)*+{\bigsqcup N_e}="v2";%
(0,15)*+{\bullet}="v3"; (30,15)*+{\bullet}="v4";%
(60,15)*+{\bullet}="v5"; (15,0)*+{A}="v6";(45,0)*+{B}="v7";%
%arrows
{\ar@{->>} "v1"; "v3"}; {\ar@{->}_{m} "v1"; "v6"};%
{\ar@{->>}^{p} "v1"; "v2"};{\ar@{->>} "v1"; "v4"};%
    {\ar@{->}_{n} "v2"; "v7"};{\ar@{->>} "v2"; "v5"};%
    {\ar@{>->}|{m''} "v3";"v6"}; {\ar@{>->}|{(fm)''} "v4"; "v7"};%
    {\ar@{->}|{n''} "v5"; "v7"};{\ar@{->}_{f} "v6"; "v7"}
\end{xy}
```

Here follows another diagram from Schubert's book (vol. II, p.39):

which was produced by the following code:
$\backslash$ begin\{xy\}

```
%vertices
(20,20)*+{Q}="v1";(40,20)*+{P_{e_j}}="v2"; (60,20)*+{\bigsqcup P_e}="v3";%
(0,0)*+{Q}="v4";(20,0)*+{\bigoplus Q_j}="v5";(40,0)*+{N}="v6";%
(70,0)*+{A}="v7";
%arrows
{\ar@{->}_{k_j} "v1";"v5"};{\ar@{->}^{v_{e_j}} "v1";"v2"};%
{\ar@{->}^{w_j} "v1";"v6"};{\ar@{->}^{h_j} "v2";"v6"};%
{\ar@{->}^{i_{e_j}} "v2";"v3"};%
    {\ar@{->}^{c_j}|<<<<<<<<<<<<{\hole} "v2";"v7"};%
{\ar@{->}^{g} "v3";"v7"};{\ar@{->}^{\Delta} "v4";"v5"};%
{\ar@{->}@/_{1.5pc}/l{w} "v4";"v6"};
{\ar@{->}^{w'} "v5";"v6"};{\ar@{->}_{i_D} "v6";"v3"};%
{\ar@{->}_{n} "v6";"v7"};
\end{xy}
```

The next diagram (figure 1) was taken from a book of algebraic topology (A User's Guide to Algebraic Topology, by Dodson and Parker [2], p. 269) and was produced by the code:

```
\newcommand{\sbol}{\small\bfseries}
\begin{xy}
%vertices
(27,0)*+{E^{[0]}=B}="v1"; (0, 20)*+{E^{[1]}}="v2"; (70,20)*+{F^{[1]}}="v3";%
(25,35)*+{K\left(\pi_1(F),1\right)}="v4";%
(95,35)*+{K\left(\pi_1(F),1\right)}="v5"; (0,45)*+{\vdots}="v6";%
(70,45)*+{\vdots}="v7"; (0,70)*+{E^{[n-1]}}="v8";%
(70,70)*+{F^{[n-1]}}="v9";%
(25,85)*+{K\left(\pi_{n-1}(F),n-1\right)}="v10";%
(95,85)*+{K\left(\pi_{n-1}(F),n-1\right)}="v11"; (-20,100)*+{E}="v12";%
(50,100)*+{F}="v13"; (0,115)*+{E^{[n]}}="v14"; (70,115)*+{F^{[n]}}="v15";%
(25,130)*+{K\left(\pi_{n}(F) ,n\right)}="v16";%
(95,130)*+{K\left(\pi_{n}(F),n\right)}="v17";
(0,150)*+{\vdots}="v18"; (70,150)*+{\vdots}="v19";
%arrows
{\ar@{->>}^{p_{n+1}} "v18"; "v14"};{\ar@{->>} "v19"; "v15"};%
{\ar@{^{(}->} "v16";"v14" };{\ar@{^{(}->} "v17";"v15" };%
```

```
{\ar@{_{(}->} "v15";"v14" };%
{\ar@{->}^{h_{n}} "v12"; "v14"};{\ar@{->}^{h'_{n}} "v13"; "v15"};%
{\ar@{_{(}->} "v13";"v12" };
{\ar@{->>}^{p_{n}}|(.33){\hole} "v14"; "v8"};%
{\ar@{->}^{h_{n-1}} "v12"; "v8"};{\ar@{->}^{h_{1}} "v12"; "v2"};%
{\ar@{->>} "v15"; "v9"};%
{\ar@{->}^{h'_{n-1}} "v13"; "v9"};{\ar@{->}_{h'_{1}} "v13"; "v3"};%
{\ar@{_{(}->} |(.18){\hole} "v9";"v8" };%
{\ar@{^{(}->} "v10";"v8" };%
{\ar@{^{(}->} "v11";"v9" };
{\ar@{->>} "v8"; "v6"};{\ar@{->>} "v9"; "v7"};%
{\ar@{->>} "v6"; "v2"};{\ar@{->>} "v7"; "v3"};%
{\ar@{^{(}->}|(.35){\hole} "v4";"v2" };%
{\ar@{^{(}->} "v5";"v3" };
{\ar@{->}"v8"; "v1"};%
{\ar@{_{(}->}|(.725){\hole} "v3";"v2" };
{\ar@{->>}_{q_1=p_1}"v2"; "v1"};%
\end{xy}
```

Finally, here it comes our version of the diagram from Valiente Feruglio ([8], see also The Latex Graphics Companion [3]). The diagram was produced by the following code:

```
\begin{xy}
%vertices
(27,0)*+{E^{[0]}=B}="v1"; (0, 20)*+{E^{[1]}}="v2"; (70,20)*+{F^{[1]}}="v3";%
(25,35)*+{K\left(\pi_1(F),1\right)}="v4";%
(95,35)*+{K\left(\pi_1(F),1\right)}="v5";%
(0,45)*+{\vdots}="v6"; (70,45)*+{\vdots}="v7"; (0,70)*+{E^{[n-1]}}="v8";%
(70,70)*+{F^{[n-1]}}="v9"; (25,85)*+{K\left(\pi_{n-1}(F),n-1\right)}="v10";%
(95,85)*+{K\left(\pi_{n-1}(F),n-1\right)}="v11"; (-20,100)*+{E}="v12";%
(50,100)*+{F}="v13"; (0,115)*+{E^{[n]}}="v14"; (70,115)*+{F^{[n]}}="v15";%
(25,130)*+{K\left(\pi_{n}(F),n\right)}="v16";%
(95,130)*+{K\left(\pi_{n}(F),n\right)}="v17";
(0,150)*+{\vdots}="v18"; (70,150)*+{\vdots}="v19";
%arrows
```



Figure 1: Moore-Postnikov's tower of a fibration [2]


```
{\ar@{->>}^{p_{n+1}} "v18"; "v14"};{\ar@{->>} "v19"; "v15"};%
{\ar@{^{(}->} "v16";"v14" };{\ar@{~{(}->} "v17";"v15" };%
{\ar@{_{(}->} "v15";"v14" };%
{\ar@{->}^{h_{n}} "v12"; "v14"};{\ar@{->}^{h'_{n}} "v13"; "v15"};%
{\ar@{_{(}->} "v13";"v12" };
{\ar@{->>}^{p_{n}}|(.33){\hole} "v14"; "v8"};%
{\ar@{->}^{h_{n-1}} "v12"; "v8"};{\ar@{->}^{h_{1}} "v12"; "v2"};%
{\ar@{->>} "v15"; "v9"};%
{\ar@{->}^{h'_{n-1}} "v13"; "v9"};{\ar@{->}_{h'_{1}} "v13"; "v3"};%
{\ar@{_{(}->} | (.18){\hole} "v9";"v8" };%
{\ar@{^{(}->} "v10";"v8" };%
{\ar@{^{(}->} "v11";"v9" };
{\ar@{->>} "v8"; "v6"};{\ar@{->>} "v9"; "v7"};%
{\ar@{->>} "v6"; "v2"};{\ar@{->>} "v7"; "v3"};%
{\ar@{^{(}->}|(.35){\hole} "v4";"v2" };%
{\ar@{^{(}->} "v5";"v3" };
{\ar@{->}"v8"; "v1"};%
{\ar@{_{(}->}|(.725){\hole} "v3";"v2" };
{\ar@{->>}_{q_1=p_1}"v2"; "v1"};%
\end{xy}
```


## References

[1] Campani, C.A.P.: Tutorial de $X_{Y}$-pic (in portuguese), 2006, available from CTAN
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