

2.3. Home and comoving frames' shared space and time dispersals

For any fixed $v = \tanh(\tau_f \alpha_f) = \tanh \underline{\tau}$, $\gamma = \cosh \underline{\tau}$, $v\gamma = \sinh \underline{\tau}$, (6) and (12) yield the rockets' HOME FRAME SHARED VELOCITY TIME AND DISTANCE DISPERSALS:

$$\Delta T \triangleq t_f - t_r = \sinh \underline{\tau} \cdot (1 + KL) - \sinh \underline{\tau} = v\gamma(1 + KL) - v\gamma = v\gamma KL, \quad (16)$$

$$\Delta D \triangleq (L + x_f) - x_r = L + (\cosh \underline{\tau} - 1) \cdot (1 + KL) - (\cosh \underline{\tau} - 1) = L(1 + K(\gamma - 1)). \quad (17)$$

Lorentz transformations yield COMOVING FRAME SHARED VELOCITY DISPERSALS:

$$\Delta \mathfrak{T} \triangleq \gamma [\Delta T - v\Delta D] = \gamma [v\gamma KL - vL(1 + K(\gamma - 1))] = -\gamma vL(1 - K), \quad (18)$$

$$\Delta \mathfrak{D} \triangleq \gamma [\Delta D - v\Delta T] = \gamma [L(1 + K(\gamma - 1)) - v^2 K \gamma L] = L [\gamma(1 - K) + K]. \quad (19)$$