The euclideangeometry package

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Preface

This file contains the documented code of euclideangeometry. The user manual source file euclideangeometry-man.tex and the readable document is euclideangeometry.pdf; it should already be installed with your updated complete TeX system installation.

Please refer to the user manual before using this package.

1 The code

1.1 Checking the date of a sufficiently recent curve2e package

This package has been already identified by the commands extracted by the docstrip package, during the .dtx file compilation. In any case, if the test checks that the curve2e file date is too old; it warns the user with an emphasised error message on the console, loading this euclideangeometry package is stopped and the whole job aborts. The emphasised error message appears like this:
1.2 Labelling

While doing any graphical geometrical drawing it is necessary to label points, lines, angles and other such items. Non measurable labels should be in upright sans serif font, according to the ISO regulations, but here we are dealing with points identified by macros that contain their (cartesian or polar) coordinates that very often are both labels and math variables.

Here we provide a versatile macro that can do several things. Its name is \Pbox and it produces a box containing the label in math format. By default the point label is typeset with the math font variant produced by command \mathsf, but the macro is sufficiently versatile to allow other settings; it accepts several optional arguments, therefore its syntax is particular:

\Pbox(\langle coordinates\rangle)[\langle alignment\rangle][\langle label\rangle][\langle diameter\rangle][\star][\langle angle\rangle]

where \langle coordinates\rangle are the coordinates where to possibly set a black dot with the specified \langle diameter\rangle; in any case it is the reference point of the \langle label\rangle; the \langle alignment\rangle is formed by the usual letters t, b, c, l, r that can be paired in a coherent way (for example the couple tb is evidently incoherent, as well as lr), but in absence of this optional specification, the couple cc is assumed; most often than not, the label position becomes such that when the user reviews the document drafts, s/he understands immediately that s/he forgot to specify some reasonable \langle alignment\rangle codes; in any case the cc code works fine to just put the dot of a specified diameter but with an empty label. Think of the \langle alignment\rangle letters as the position of the reference point with respect to the \langle label\rangle optical
center. The optional \textit{angle} argument produces a rotation of the whole label by that angle; it may be used in several circumstances, especially when the label is just text, to produce, for example, a sideways legend. It is useful also when the labels are produced within a rotated box, in order to counterrotate them.

The optional asterisk draws a frame around the label. Notice that the separator between the visible or the invisible frame and the box contents varies according the the fact that the \textit{alignment} specification contains just one or two letter codes; this is useful, because the diagonal position of the label should be optically equal to the gap that exists between the reference point and the \textit{label} box.

If the \textit{diameter} is zero, no dot is drawn, the whole \textit{label} is typeset with the mathit math font; otherwise only the first symbol of a math expression is typeset in sans serif. The presence of subscripts makes the labels appear more distant from their reference point; the same is true when math symbols, even without subscripts, are used, because of the oblique nature of the math ‘letters’ alphabet.

If some text has to be printed as a label, it suffices to surround it with dollar signs, that switch back to text mode when the default mode is the math one. With this kind of textual labels it might be convenient to use the optional asterisk to frame the text. The final optional argument \textit{angle} (to be delimited with the \texttt{\textless} \texttt{\textgreater} signs) specifies the inclination of the label with respect to the horizontal line; it is useful, for example to set a label along a sloping line.

\providecommand\Pbox{}
\newlength\PbDim
\RenewDocumentCommand\Pbox{D(){0,0} O{cc} m O{0.5ex} s D<>{0}}{\put(#1){\rotatebox{#6}{\makebox(0,0){\settowidth\PbDim{#2}\edef\Rapp{\fpeval{\PbDim/{1ex}}}\fptest{\Rapp > 1.5}{\fboxsep=0.5ex}{\fboxsep=0.75ex}\IfBooleanTF{#5}{\fboxrule=0.4pt}{\fboxrule=0pt}\fptest{#4 = 0sp}{\makebox(0,0)\[#2\]{\fbox{$\relax#3\relax$}}}\edef\Diam{\fpeval{(#4)/\unitlength}}\makebox(0,0){\circle*{\Diam}}\makebox(0,0)\[#2\]{\fbox{$\relax\mathsf#3\relax$}}}}\}}}%\ignorepaces}

The following command, to be used always within a group, or an environment or inside a box, works only with piecewise continuously scalable font collection, such as, for example, the Latin Modern fonts, or with continuously scalable fonts, such as, for example, the Times ones. They let the operator select, for the scope of the command, any size, even fractional so as to fine adjust the text width in the space allowed for it; it is particularly useful with the monospaced fonts, that forbid hyphenation, and therefore cannot be adjusted to the current line width.

\DeclareRobustCommand\setfontsize[2][1.2]{\linespread{#1}\fontsize{#2}{#2}\selectfont}

With OpenType fonts there should not be any problems even with math fonts;
with Type 1 fonts the only scalable fonts I know of, are the LibertinusMath fonts, usable through the LibertinusT1math package, are also the only ones that have 8 bit encoded math fonts (256 glyph fonts), while the standard default Type 1 math fonts are just 7 bit encoded (128 glyphs fonts).

Another useful labelling command is \texttt{Zbox}; this command is an evolution of a command that I been using for years in several documents of mine. It uses some general text, not necessarily connected to a particular point of the \texttt{picture} environment, as a legend; It can draw short text as a simple horizontal box, and longer texts as a vertical box of specified width and height.

Is syntax is the following:

\[
\texttt{Zbox(position)((()))dimensions}[(alignment)]{(text)}
\]

where \texttt{position} is where the reference point of the box has to be put in the picture; \texttt{dimensions} are optional; if not specified, the box is a horizontal one, and it is as wide as its contents; if it is specified, it must be a comma separated list of two integer or fractional numbers that are the width and the height of the box; if the height is specified as zero, the width specifies a horizontal box of that width; \texttt{alignment} is optional and is formed by one or two coherent letter codes from the usual set \texttt{t, b, c, l, r}; if the \texttt{alignment} is absent, the default alignment letters are \texttt{bl}, i.e. the box reference point is the bottom left corner; \texttt{text} contains general text, even containing some math.

\begin{verbatim}
\def\EUGsplitArgs(#1,#2)#3#4{\edef#3{#1}\edef#4{#2}}
\newlength\EUGZbox
\providecommand\Zbox{}
\RenewDocumentCommand\Zbox{r() D(){0,0} O{bl} m}{% 
\EUGsplitArgs(#2)
\ZboxX\ZboxY % splits box dimensions
\fboxsep=2\unitlength
\ifnum\ZboxX=\z@ 
\def\ZTesto{\fbox{#4}}% 
\else 
\ifnum\ZboxY=\z@ 
\def\ZTesto{\fbox{\parbox{\ZboxX\unitlength}{#4}}}% 
\else 
\def\ZTesto{% 
\setbox\EUGZbox=\hbox{\fbox{% \parbox[c][\ZboxY\unitlength][c]{\ZboxX\unitlength}{#4}}}% 
\dimen\EUGZbox=\dimexpr(\ht\EUGZbox +\dp\EUGZbox)/2\relax 
\ht\EUGZbox=\dimen\EUGZbox\relax 
\dp\EUGZbox=\dimen\EUGZbox\relax 
\box\EUGZbox% 
}% 
\fi 
\fi 
\put(#1){\makebox(0,0)[#3]{\ZTesto}}\ignorespaces}
\end{verbatim}
1.3 Service macros for ellipses

The `ellisse` has a control sequence name in Italian; it differs for just one letter from the name `ellipse` English name, but we cannot use the latter one because it may conflict with other packages loaded by the user; actually this command and the next one are just shortcuts for executing more general commands with specific sets of arguments. For details and syntax, please refer yourself to section 1.6.

\begin{verbatim}
\NewDocumentCommand{ellisse}{s m m}{\IfBooleanTF{#1}{\let\fillstroke\fillpath}{\let\fillstroke\strokepath}\Sellisse[#2]{#3}}
\NewDocumentCommand{Xellisse}{s D(){0,0} O{0} m m O{} o}{\IfBooleanTF{#1}{\ XSellisse*(#2)[#3]{#4}{#5}[#6][#7]}{\ XSellisse(#2)[#3]{#4}{#5}[#6][#7]}}
\end{verbatim}

We do not know if the following macro `polyvector` may be useful for euclidean geometry constructions, but it may be useful in block diagrams; it is simply a polyline where the last segment is a geometrical vector. As in polyline the number of recursions is done until the last specified coordinate pair; recognising that it is the last one, instead of drawing a segment, the macro draws a vector.

\begin{verbatim}
def\polyvector(#1){\roundcap\def\EUGpreviouspoint{#1}\EUGpolyvector}
def\EUGpolyvector(#1){\@ifnextchar({\segment(\EUGpreviouspoint)(#1)\def\EUGpreviouspoint{#1}\EUGpolyvector}{\VECTOR(\EUGpreviouspoint)(#1)}}
\end{verbatim}

1.4 Processing lines and segments

The next macros are functional for the geometric constructions we are going to make: finding the intersection of lines or segments, finding the lengths and arguments of segments, directions, distances, distance of a point from a line or a segment, the symmetrical point of another one specified with respect to a given center of symmetry; the axes of segments, the solutions of the relationship between the semi axes of an ellipse and the semi focal distance, and so on.

Most of these commands have delimited arguments; the delimiters may be the usual parentheses, but they may be keywords; many commands contain the keyword `to`, not necessarily the last one; the arguments before such keyword may be entered as ordered comma separated numerical couples, or comma separated macros the containing scalar values; or they may be macros that contain the ordered couples representing vectors or directions; they all may be in cartesian or
polar form. Remember that such ordered couples are complex numbers, representable by vectors applied to the origin of the axes; therefore sometimes it is necessary that the underlying commands execute some vector differences so as to work with generic vectors.

On the opposite the output values, i.e. the argument after that to keyword, should be tokens that can receive a definition, in general macros, to which the user should assign a mnemonic name; s/he should use such macros for further computations or for drawing commands.

The first and principal command is \texttt{\textbackslash IntersectionOfLines} and it has the following syntax:

\begin{verbatim}
\textbackslash IntersectionOfLines((point1))(\langle dir1\rangle)\text{\textbackslash and}(\langle point2\rangle)(\langle dir2\rangle)\text{\textbackslash to}(crossing)
\end{verbatim}

where \texttt{(point1)} and \texttt{(dir1)} are respectively a point of the first line and its direction, not a second point, but the direction — it is important to stress this point; similarly for the second line; the output is stored in the macro that identifies the \texttt{(crossing)} point. The directions do not need to be expressed with unit vectors, but the lines must not be parallel or anti parallel (equal directions or differing by \(180^\circ\)); the macro contains a test that checks this anomalous situation because an intersection at infinity or too far away (\(2\times10^{14}\) typographical points, approximately 5,758 m) is of no interest; in case, no warning message is issued, the result is put to 0,0, and the remaining computations become nonsense. It is a very unusual situation and I never encountered it; nevertheless...

\begin{verbatim}
def\IntersectionOfLines(#1)(#2)\text{\textbackslash and}(#3)(#4)\text{\textbackslash to}(#5){\bgroup
\def\IntPu{#1}\def\Uu{#2}\def\IntPd{#3}\def\Ud{#4}\%
\DirOfVect\Uu\text{\textbackslash to}\Du
\DirOfVect\Ud\text{\textbackslash to}\Dd
\XpartOfVect\Du\text{\textbackslash to}\a\ \YpartOfVect\Du\text{\textbackslash to}\b
\XpartOfVect\Dd\text{\textbackslash to}\c\ \YpartOfVect\Dd\text{\textbackslash to}\d
\XpartOfVect\IntPu\text{\textbackslash to}\xu\ \YpartOfVect\IntPu\text{\textbackslash to}\yu
\XpartOfVect\IntPd\text{\textbackslash to}\xd\ \YpartOfVect\IntPd\text{\textbackslash to}\yd
\edef\Den{\texttt{fpeval}{-(\a*\d-\b*\c)}}%
\fptest{\texttt{abs}(\Den)<1e-5}\{% Almost vanishing determinant
\def#5{0,0}%
\} % Determinant OK
\edef\Numx{\texttt{fpeval}{(\d*(\b*\xu-\a*\yu)-\a*(\d*\xd-\c*\yd))/\Den}}%
\edef\Numy{\texttt{fpeval}{(\c*(\b*\xu-\a*\yu)-\b*(\d*\xd-\c*\yd))/\Den}}%
\CopyVect\Numx,\Numy\text{\textbackslash to}\Paux
\edef\x{\texttt{group}\texttt{noexpand}edef\texttt{noexpand}#5\{\Paux\}}\texttt{x}\texttt{ignorespaces}}
\end{verbatim}

The \texttt{\textbackslash IntersectionOfSegments} macro is similar but in input it contains the end points of two segments: internally it uses \texttt{\textbackslash IntersectionOfLines} and to do so it has to determine the directions of both segments. The syntax is the following:

\begin{verbatim}
\textbackslash IntersectionOfSegments((point11))(\langle point12\rangle)\text{\textbackslash and}(\langle point21\rangle)(\langle point22\rangle)\text{\textbackslash to}(crossing)
\end{verbatim}
The \textit{(crossing)} point might fall outside one or both segments. It is up to the users to find out if the result is meaningful or nonsense. Two non parallel lines are infinitely long in both directions and any \textit{(crossing)} point is acceptable; with segments the situation might become nonsense.

\begin{verbatim}
def\IntersectionOfSegments(#1)(#2)and(#3)(#4)to#5{% \SubVect#1from#2to\IoSvectu \DirOfVect\IoSvectu to\DirIoSVecu \SubVect#3from#4to\IoSvectd \DirOfVect\IoSvectd to\DirIoSVecd \IntersectionOfLines(#1)(\DirIoSVecu)and(#3)(\DirIoSVecd)to#5\ignorespaces}
\end{verbatim}

An application of the above intersections is formed by the next two macros; they find the axes of a couple of sides of a triangle and use their base point and direction to identify two lines the intersection of which is the circumcenter; the distance of one base point from the circumcenter is the radius of the circumcircle that can be drawn with the usual macros. We have to describe the macros \texttt{\textbackslash AxisOf} and \texttt{\textbackslash CircleWithCenter} and we will do it in a little while. Meanwhile the syntax of the whole macro is the following:

\begin{verbatim}
\ThreePointCircle{\star}(\vertex1)(\vertex2)(\vertex3)
\end{verbatim}

where the three vertices are the three points where the circle must pass, but they identify also a triangle. Its side axes intersect in one point that by construction is at the same distance from the three vertices, therefore it is the center of the circle that passes through the three vertices. A sub product of the computations is the macro \texttt{\textbackslash C} that contains the center coordinates. If the optional asterisk is used the whole drawing is executed, while if it is missing, only the \texttt{\textbackslash C} macro remains available but the user is responsible to save/copy its value into another macro; for this reason another macro should be more easy to use; its syntax is the following:

\begin{verbatim}
\ThreePointCircleCenter{\star}(\vertex1)(\vertex2)(\vertex3)
\end{verbatim}

where the vertices have the same meaning, but \texttt{(center)} is the user chosen macro that contains the center coordinates.

\begin{verbatim}
\NewDocumentCommand\ThreePointCircle{s r() r() r()}{% \AxisOf#2and#3to\Mu\Du \AxisOf#2and#4to\Md\Dd \IntersectionOfLines(\Mu)(\Du)and(\Md)(\Dd)to\C \SubVect#2from\C to\R \IfBooleanTF{#1}{\CircleWithCenter\C Radius\R}{\ignorespaces}
\end{verbatim}

\begin{verbatim}
\ThreePointCircleCenter{r() r() r()}\vertex1(\vertex2)(\vertex3)
\end{verbatim}

where \texttt{(center)} is the user chosen macro.

\begin{verbatim}
\NewDocumentCommand\ThreePointCircleCenter{r() r() r()}\vertex1(\vertex2)(\vertex3){% \ThreePointCircle(#1)(#2)(#3)\CopyVect\C to#4}
\end{verbatim}

There are some useful commands that help creating picture diagrams in an easier way; for example one of the above described commands internally uses \texttt{\textbackslash CircleWithCenter}. It is well known that the native \texttt{\textbackslash circle} command \texttt{\textbackslash circle} requires the specification of the diameter but many \texttt{euclideangeometry} commands already get the distance of two points, or the magnitude of a segment,
or similar objects that may be used as a radius, rather than the diameter; why should we not have macros that simultaneously compute the require diameter and draw the circle. Here there are two such macros; they are similar to one another but their names differ in capitalisation, but also in the way they use the available input information. The syntax is the following:

```
\CircleWithCenter{center} Radius{Radius}
\Circlewithcenter{center} radius{radius}
```

where in both cases \textit{\{center\}} is a vector/ordered couple that points to the circle center. On the contrary \textit{\{Radius\}} is a vector obtained through previous calculations, while \textit{\{radius\}} is a scalar containing a previously calculated length.

```
def\CircleWithCenter#1Radius#2{\put(#1){\ModOfVect#2to\CWR\circle{\fpeval{2*\CWR}}}\ignorespaces}
def\Circlewithcenter#1radius#2{\put(#1){\circle{\fpeval{2*abs(#2)}}}\ignorespaces}
```

As announced, here we have a macro to compute the axis of a segment; given two points $P_1$ and $P_2$, for example the end points of a segment, or better the end point of the vector that goes from $P_1$ to $P_2$, the macro determines the segment middle point and a second point the lays on the perpendicular at a distance equal to half the first two points distance; this second point lays at the left of vector $P_2 - P_1$, therefore it is important to select the right initial vector, in order to have the second axis point on the desired side.

```
\AxisOf{P1}and{P2}to\{Axis1\}{Axis2}
```

Macros \textit{\SegmentCenter} and \textit{\MiddlePointOf} are alias of one another; their syntax is:

```
\SegmentCenter((P1))((P2))to\{center\}
\MiddlePointOf((P1))((P2))to\{center\}
```

\textit{\{P1\}}, \textit{\{p2\}} and \textit{\{center\}} are all vectors.

```
def\AxisOf#1and#2to#3#4{%
\SubVect#1from#2to\Base\ScaleVect\Base by0.5to\Base
\AddVect\Base and#1to#3\MultVect\Base by0,1to#4
}
def\SegmentCenter(#1)#2to#3{\AddVect#1and#2to\Segm\ScaleVect\Segm by0.5to#3\ignorespaces}
\let\MiddlePointOf\SegmentCenter
```

Some other macros are needed to solve certain triangle problems; one of such macros is the one allows to determine the length of one leg of a right triangle by knowing the lengths of the hypotenuse and the other leg. The syntax is the following:
where the three parameters may be macros, especially the last one; all of them contain scalar values.

\Leftrightarrow\\LegFromHypotenuse\AndOtherLeg{leg1}to\{leg2}\rangle

Another useful macro determines the two intersections of a line with a circumference if they exist; otherwise it issues a warning and sets both output values to vector 0,0, which, of course, is wrong, but it allows to go on with typesetting, although with non-sense results. Warnings do not stop the compilation program, therefore their message goes to the .log file and the user might not notice it; but since the results are probably absurd, s/he certainly notice this fact and look for messages; the user, therefore, who has carefully read this user manual, immediately looks onto the .log file and realises the reason of the wrong results.

The syntax of this macro is the following:

\IntersectionsOfLine(point)(direction)WithCircle(center){radius}to\{int1\}and\{int2\}

where \{point\} and \{direction\} are the line parameters that can be explicit complex values or macros; \{center\} is the circumference explicit complex value, or a macro, containing the center coordinates; \{radius\} is the scalar explicit or macro radius length; The intersection points \{int1\} and \{int2\} are supposed to be macros that get defined with the intersection point coordinates; \{int1\} is the first intersection that is determined along the line \{direction\}. Please notice the different first part of the macro name \IntersectionsOfLine compared to the macro that determines the intersection of two lines \IntersectionOfLines: two intersections and one line vs. one intersection with two lines.
where, as usual, the input data may be explicit or macro defined coordinates, while the output result should be a macro name.

Another useful macro draws a circle given its (center) and the coordinates of the (point) which the circumference should pass through. The syntax is:

\CircleThrough{\langle point \rangle} WithCenter{\langle center \rangle}

As usual, the parameters are all explicit or macro defined complex numbers.

The above macro is the building block for a simple macro that draws two circles that cross at a given point; but it is so simple that it is not worth defining a macro: if the user wants to try his/her ability, s/he may define:

\NewDocumentCommand{r() r() r()}{\CircleThrough{\langle point \rangle} WithCenter{\langle center \rangle}}
\CircleThrough{\langle point \rangle} WithCenter{\langle center \rangle} \ignorespaces

where \ignorespaces may be superfluous, but is always a safety action when defining commands to be used within the picture environment. In any case see example XXX in euclideangeometry-man.pdf

### 1.5 Triangle special points

Here we have the macros to find the special points on a triangle side that are the “foot” of special lines from one vertex to the opposite side. We already described the circumcircle and the circumcenter, but that is a separate case, because the circumcenter is not the intersection of special lines from one vertex to the opposite base. The special lines we are interested in here are the height, the median, and the bisector The macros have the same aspect \Triangle...Base, where the dots are replaced with each of the (capitalised) special line names. Their syntaxes are therefore very similar:

\TriangleMedianBase{\langle vertex \rangle} on{\langle base1 \rangle} and{\langle base2 \rangle} to{\langle M \rangle}
\TriangleHeightBase{\langle vertex \rangle} on{\langle base1 \rangle} and{\langle base2 \rangle} to{\langle H \rangle}
\TriangleBisectorBase{\langle vertex \rangle} on{\langle base1 \rangle} and{\langle base2 \rangle} to{\langle B \rangle}

where (vertex) contains one of the vertices coordinates, and (base1) and (base2) are the end points of the side opposite to that triangle vertex; (M), metaH, and (B) are the intersections of these special lines from the (vertex) to the opposite
side; in order, they are the foot of the median, the foot of the height; the foot of the bisector. The construction of the median foot $M$ is trivial because this foot is the base center; the construction of the height foot is a little more complicated, because it is necessary to find the exact direction of the perpendicular from the vertex to the base in order to find the intersection $H$; the construction of the bisector base implies finding the exact direction of the two sides starting at the vertex, and taking the mean direction, which is trivial if polar coordinates are used; at this point the bisector line is completely determined and the intersection with the base line $B$ is easily obtained.

143 \def\TriangleMedianBase#1on#2and#3to#4{\% 144 \SubVect#1from#2to\TMBu \SubVect#1from#3to\TMBd 145 \SubVect\TMBu from\TMBd to\Base 146 \ScaleVect\Base by0.5to\TMBm \AddVect#2and\TMBm to#4\ignorespaces} 148 \% 149 \def\TriangleHeightBase#1on#2and#3to#4{\% 150 \SubVect#2from#3to\Base 151 \ArgOfVect\Base to\Ang \CopyVect\fpeval{\Ang+90}:1 to\Perp 152 \IntersectionOfLines(#1)(\Perp)and(#2)(\Base)to#4\ignorespaces} 153 \% 154 \def\TriangleBisectorBase#1on#2and#3to#4{\% 155 \SubVect#2from#3to\Base 156 \SubVect#2from#1to\Luno \SubVect#3from#1to\Ldue 157 \ArgOfVect\Luno to\Arguno \ArgOfVect\Ldue to\Argdue 158 \edef\ArgBis{\fpeval{\Arguno+\Argdue/2}}\% 159 \CopyVect \ArgBis:1to \Bisect 160 \IntersectionOfLines(#2)(\Base)and(#1)(\Bisect)to#4\ignorespaces} 164 \let\TriangleCircumcenter\ThreePointCircleCenter 165 \let\TriangleCircummcircle\ThreePointCircle 169 Having defined the previous macros, it becomes very easy to create the macros to find the \textit{barycenter}; the \textit{orthocenter}, the \textit{incenter}; for the \textit{circumcenter} and the \textit{circumcircle} we have already solved the question with the \ThreePointCircleCenter and the \ThreePointCircle macros; for homogeneity, we create here their aliases with the same form as the new “center” macros. Actually, for the “circle” macros, once the center is known, there is no problem with the circumcircle, while for the incircle it suffices a macro to determine the distance of the incenter from one of the triangle sides; such a macro is going to be defined in a little while; it is more general than simply to determine the radius of the incircle.

161 \let\TriangleCircumcenter\ThreePointCircleCenter 163 \let\TriangleCircummcircle\ThreePointCircle 169 The other “center” macros are the following; they all consist in finding two of the specific triangle lines, and finding their intersection. Therefore for the barycenter we intersect two median lines; for the orthocenter we intersect two height lines; for the incenter we intersect two bisector lines; 164 \def\TriangleBarycenter(#1)(#2)(#3)to#4\% 166 \TriangleMedianBase#1on#2and#3to\Pa 167 \TriangleMedianBase#2on#3and#1to\Pb
1.6 Other specific service macros

And here it comes the general macro to determine the distance of a point from a segment or from a line that contains that segment; it may be used for determining the radius of the incenter, but it is going to be used also for other purposes. Its syntax is the following:

\[ \text{DistanceOfPoint}(\text{point}) \text{ from}(\langle P1 \rangle)(\langle P2 \rangle)\text{to}(\text{distance}) \]

where \( \text{point} \) is a generic point; \( \langle P1 \rangle \) and \( \langle P2 \rangle \) are a segment end points, or two generic points on a line; \( \text{distance} \) is the macro that receives the computed scalar distance value.

\[ \text{DistanceOfPoint}(\text{point})\text{ from}(\langle P1 \rangle)(\langle P2 \rangle)\text{to}(\text{distance}) \]

The following macros are specific to solve other little geometrical problems that arise when creating more complicated constructions.

The \texttt{AxisFromAxisAndFocus} is an unhappy name that describes the solution of an ellipse relationship between the ellipse axes and the focal distance

\[ a^2 = b^2 + c^2 \]  \hspace{1cm} (1)

This relation exists between the “semi” values, but it works equally well with the full values. Evidently \( a \) is the largest quantity and refers to the main ellipse axis, the one that passes through the two foci; \( b \) refers to the other shorter ellipse axis and \( c \) refers to the foci; \( b \) and \( c \) are smaller than \( a \), but there is no specific relationship among these two quantities. It goes by itself that these statements

\[ a^2 = b^2 + c^2 \]  \hspace{1cm} (1)
apply to a veritable ellipse, not to a circle, that is the special case where \( b = a \) and \( c = 0 \).

Since to solve the above equation we have one unknown and two known data, but we do not know what they represent, we have to assume some relationship exist between the known data; therefore if \( a \) is known it must be entered as the first macro argument; otherwise \( a \) is the unknown and the first Argument has to be the smaller one among \( b \) and \( c \). Since \( b \) and \( c \) may come from other computation the user has a dilemma: which is the smaller one? But this is a wrong approach; of course if the user knows which is the smaller, s/he can use the macro by entering the data in the proper order; but the user is determining the main axis, therefore it better that s/he uses directly the second macro \texttt{MainAxisFromAxisAndFocus} that directly computes \( a \) disregarding the order with which \( b \) and \( c \) are entered; the macro name suggests to enter \( b \) first and \( c \) second, but it is irrelevant thanks to the sum properties. Summarising:

- if the main axis is known use \texttt{AxisFromAxisAndFocus} by entering the main axis as the first argument; otherwise
  - if it is known which is smaller among \( b \) and \( c \), it is possible to use \texttt{AxisFromAxisAndFocus} by entering the smaller one as the first argument; otherwise
  - determine the main axis by using \texttt{MainAxisFromAxisAndFocus}

Their syntaxes of these two commands are basically the following:

\[
\texttt{AxisFromAxisAndFocus}(\texttt{main axis}) \ \texttt{and}(\texttt{axis or focus}) \ \texttt{to}(\texttt{focus or axis})
\]
\[
\texttt{MainAxisFromAxisAndFocus}(\texttt{axis or focus}) \ \texttt{and}(\texttt{focus or axis}) \ \texttt{to}(\texttt{main axis})
\]

but it is possible to enter the data in a different way with the first command; the described syntax is the suggested one. Evidently \( \texttt{axis or focus} \) and \( \texttt{focus or axis} \) imply that if you specify the focus in one of the two, you have to specify the axis in the other one.

191 \texttt{\def\AxisFromAxisAndFocus#1and#2to#3{%}
192 \texttt{\fptest{abs(#1)>abs(#2)}\}%
193 \texttt{\{\edef#3{\fpeval{sqrt(#1**2-#2**2)}}\}}%
194 \texttt{\{\edef#3{\fpeval{sqrt(#2**2+#1**2)}}\}}%
196 \texttt{\def\MainAxisFromAxisAndFocus#1and#2to#3{%}
197 \texttt{\edef#3{\fpeval{sqrt(#2**2+#1**2)}}\}}%
198 \texttt{\def\MainAxisFromAxisAndFocus#1and#2to#3{%}
199 \texttt{\edef#3{\fpeval{sqrt(#2**2+#1**2)}}\}}%

The following macros allow to determine some scalar values relative to segments; in the second one the order of the segment end points is important, because the computed argument refers to the vector \( P_2 - P_1 \). Their syntaxes are the following:

\[
\texttt{SegmentLength}(\langle P1 \rangle)(\langle P2 \rangle) to(length)
\]
\[
\texttt{SegmentArg}(\langle P1 \rangle)(\langle P2 \rangle) to(argument)
\]
Both \(\text{〈length〉}\) and \(\text{〈argument〉}\) are macros that contain scalar quantities; the argument is in the range \(-180^\circ < \Phi \leq +180^\circ\).

\[
def\text{SegmentLength}(\text{#1})(\text{#2})\text{to}\text{#3}\{\SubVect\text{#1from}\text{#2to}\Segm\ \text{to}\text{#3}\}
\]

\[
def\text{SegmentArg}(\text{#1})(\text{#2})\text{to}\text{#3}\{\SubVect\text{#1from}\text{#2to}\Segm\ \GetCoord(\Segm)\SegmX\SegmY\edef\text{#3}{\fpeval{\atand(\SegmY,\SegmX)}}\%
\ignorespaces}
\]

In the following sections we need some transformations, in particular the affine shear one. The macros we define here are not for general use, but are specific for the purpose of this package.

The first macro shears a segment, or better a vector that goes from point \(P_1\) to point \(P_2\) with a horizontal shear factor/angle \(\alpha\); the origin of the vector does not vary and remains \(P_1\) but the arrow tip of the vector is moved according to the shear factor; in practice this shearing macro is valid only for vectors that start from any point laying on the \(x\) axis. The shear factor \(\alpha\) is the angle of the \textit{clockwise} rotation vector operator by which the vertical coordinate lines get rotated with respect to their original position. The syntax is the following:

\[
\text{ShearVect}(\langle P1 \rangle)(\langle P2 \rangle)\text{by}\langle\text{shear} \rangle\text{to}\langle\text{vector} \rangle
\]

where \(\langle P1 \rangle\) and \(\langle P2 \rangle\) are the initial and final points of the vector to be sheared with the \(\langle\text{shear} \rangle\) angle, and the result is put in the output \(\langle\text{vector} \rangle\)

\[
def\text{ShearVect}(\text{#1})(\text{#2})\text{by}\text{#3}\text{to}\text{#4}\{\SubVect\text{#1from}\text{#2to}\AUX\%
\GetCoord(\AUX)\AUX\Auy\edef\AUX{\fpeval{\AUX + \text{#3}\times\Auy}}\%
\edef\Auy{\fpeval{\Auy}}\%
\AddVect\AUX,\Auy and\#1\text{to}\text{#4}\ignorespaces}
\]

Again we have another different \texttt{ScaleVector} macro that takes in input the starting and ending points of a vector, and scales the vector independently of the initial point.

\[
def\text{ScaleVector}(\text{#1})(\text{#2})\text{by}\text{#3}\text{to}\text{#4}\{\SubVect\text{#1from}\text{#2to}\AUX\%
\ScaleVect\AUX\text{by}\text{#3}\text{to}\AUX\%
\AddVect\AUX,\AUX\text{by}\text{#3}\text{to}\text{#4}\ignorespaces}
\]

The following macro to draw a possibly sheared ellipse appears complicated; but in reality it is not much different from a “normal” ellipse drawing command. In order to do the whole work the ellipse center is set in the origin of the axes, therefore it is not altered by the shearing process; everything else is horizontally sheared by the shear angle \(\alpha\). In particular the 12 nodes and control point that are
required by the Bézier splines that draw the four ellipse quarters. It is this multitude of shearing commands that makes the macro much longer and apparently complicated. The syntax is the following:

\Sellisse\{<h-axis>\}\{<v-axis>\}\{<shear>\}

where the optional asterisk is used to mark and label the Bézier spline nodes and the control points of the possibly sheared ellipse; without the asterisk the ellipse is drawn without any “decoration”; the optional \langle shear \rangle is as usual the angle of the sheared vertical coordinate lines; its default value is zero.

\NewDocumentCommand\Sellisse{s m m O{0}}{\bgroup
\CopyVect#2,#3to\Ptr \ScaleVect\Ptr by-1to\Pbl
\CopyVect#2,-#3to\Pbr \ScaleVect\Pbr by-1to\Ptl
\edef\Ys{\fpeval{\tand\{#4\}}}\%
\edef\K{\fpeval{4*(\sqrt(2)-1)/3}}\%
\ShearVect(0,0)(0,#3)by\Ys to\Pmt
\ShearVect(0,0)(0,-#3)by\Ys to\Pmb
\ShearVect(0,0)(#2,0)by\Ys to\Pmr
\ShearVect(0,0)(-#2,0)by\Ys to\Pml
\ShearVect(\Pmr)(\Ptr)by\Ys to\Ptr
\ShearVect(\Pml)(\Ptl)by\Ys to\Ptl
\ShearVect(\Pmr)(\Pbr)by\Ys to\Pbr
\ShearVect(\Pml)(\Pbl)by\Ys to\Pbl
\IfBooleanTF{#1}{\Pbox(\Ptr)[bl]{P_{tr}}\Pbox(\Pbl)[tr]{P_{bl}}\Pbox(\Pbr)[tl]{P_{br}}\Pbox(\Ptl)[br]{P_{tl}}\polygon(\Pbr)(\Ptr)(\Ptl)(\Pbl)}{\%
\ScaleVector(\Pmr)(\Ptr)by\K to\Crt
\ScaleVector(\Pmr)(\Pbr)by\K to\Crb
\ScaleVector(\Pml)(\Ptl)by\K to\Clt
\ScaleVector(\Pml)(\Pbl)by\K to\Clb
\ScaleVector(\Pmr)(\Ptl)by\K to\Crt
\ScaleVector(\Pmr)(\Pbr)by\K to\Crb
\ScaleVector(\Pml)(\Pbl)by\K to\Clb
\IfBooleanTF{#1}{\Pbox(\Crt)[l]{C_{rt}}\Pbox(\Crb)[l]{C_{rb}}\Pbox(\Clt)[r]{C_{lt}}\Pbox(\Clb)[r]{C_{lb}}\Pbox(\Crt)[b]{C_{tr}}\Pbox(\Crb)[b]{C_{rb}}\Pbox(\Clt)[t]{C_{tl}}\Pbox(\Clb)[t]{C_{tl}}}{\%
\endgroup}
This user macro is used to call the \Sellisse macro with the desired parameters, but also to act with it on order to fill or stroke the ellipse contour, and to select some settings such as the contour line thickness, or the color of the ellipse contour or interior. The syntax is the following:

\XSellisse\,(\langle center\rangle)\,[\langle angle\rangle] <\langle shear\rangle> \{\langle h-axis\rangle\}{\langle v axis\rangle}\,\langle*2\rangle\,[\langle settings1\rangle]\,[\langle settings2\rangle]

where there are two optional asterisks, \,(\langle*1\rangle) and \,(\langle*2\rangle); the first one controls the coloring of the ellipse: if present the interior is filled, if absent the contour is stroked; the second one controls the way a possibly sheared ellipse appears: if present, the construction is shown, if absent only the final result is shown; \,(\langle center\rangle) is optional: if present, the ellipse center is specified; if absent, its center is at the origin of the picture axes; \,(\langle angle\rangle) is optional with default value zero: if absent, the ellipse is not rotated and the \,(\langle h-axis\rangle) remains horizontal, while the \,(\langle v-axis\rangle) remains vertical, while if present and with a non vanishing value, the ellipse is rotated counterclockwise the amount specified, and, of course, if the value is negative, the rotation is clockwise. The optional parameter \,(\langle shear\rangle), if present, shears the ellipse parallel the \,(\langle h-axis\rangle) direction; the \,(\langle settings1\rangle) and \,(\langle settings2\rangle) operate as described for command \Sellisse.

1.7 Regular polygons and special ellipses

We finally arrive to more complex macros used to create special polygons and special ellipses.
1.7.1 Regular polygons

Regular polygons are not that special; it is possible to draw them by using the `\multiput` or `\xmultiput` commands, but a single command that does everything by itself with more built in functionalities is much handier. The new command `\RegPolygon` has the following syntax:

\RegPolygon\{\star\}\{center\}\{radius\}\{number\}\{angle\}\{settings\}

where \(\star\) is an optional asterisk; its presence means that the polygon interior is filled, instead of the polygon contour being stroked; the \{center\} specification of the polygon is optional; if it is omitted, the polygon center goes to the origin of the picture coordinates; \{radius\} is the mandatory radius of the circumscribed circle, or, in other words, the distance of each polygon vertex form the \{center\}; the mandatory \{number\} is an integer that specifies the number of polygon sides; the first vertex that is being drawn by this command, has an angle of zero degrees with respect to the \{center\}; if a different initial \{angle\} different from zero is desired, it is specified through this optional argument; possibly the angle bracketed optional \{setting\} parameter may be used to specify, for example, the line thickness for the contour, and/or the color for the polygon contour or interior. See the documentation `euclideangeometry-man.pdf` for more information and usage examples.

\begin{verbatim}
\newcount\RPI
\NewDocumentCommand\RegPolygon{s D(){0,0} m m O{0} D<>{\relax} }{{\%\countdef\RPI=258\%\RPI=0\%\CopyVect#5:#3to\P\%\CopyVect\fpeval{360/#4}:1to\R\%\put(#2){#6\relax\%\moveto(\P)\fpdowhile{\RPI < #4}\%\{\MultVect\P by\R to\P\%\lineto(\P)\advance\RPI by 1\%\IfBooleanTF{#1}\%{\fillpath}{#6\strokepath}}}\ignorespaces\%\def\DirOfVect#1to#2{\GetCoord(#1)\t@X\t@Y\%\ModOfVect#1to\@tempa\%\unless\ifdim\@tempa\p@=\z@\%\DividE\t@X by\@tempa to\t@X\%\DividE\t@Y by\@tempa to\t@Y\%\MakeVectorFrom\t@X\t@Y to#2\ignorespaces\%}
\end{verbatim}

1.7.2 The Steiner ellipse

The construction of the Steiner ellipse is very peculiar; it is almost intuitive that any triangle has infinitely many internal tangent ellipses; therefore it is necessary to state some other constraints to find one specific ellipse out from this unlimited set.
One such ellipse is the Steiner one, obtained by adding the constraint that the ellipse be tangent to the median points of the triangle sides. But one thing is the definition, and another totally different one is to find the parameters of such an ellipse; and working with ruler and compass, it is necessary to find a procedure to draw such an ellipse.

The construction described here and implemented with the \texttt{SteinerEllipse} macro is based on the following steps, each one requiring the use of some of the commands and/or transformations described in the previous sections.

1. Given a generic triangle (the coordinates of its three vertices) it is not necessary, but it is clearer to explain, if the triangle is shifted and rotated so as to have one of its sides horizontal, and the third vertex in the upper part of the picture drawing. So we first perform the initial shift and rotation and memorise the parameters of this transformation so that, at the end of the procedure, we can put back the triangle (and its Steiner ellipse) in its original position. Let us call this shifted and rotated triangle with the symbol $T_0$.

2. We transform $T_0$ with an affine shear transformation into an isosceles triangle $T_1$ that has the same base and the same height as $T_0$. We memorise the shear “angle” so as to proceed to an inverse transformation when the following steps are completed: let be $\alpha$ this shear angle; geometrically it represents the angle of the sheared vertical coordinate lines with respect to the original vertical position.

3. With another affine vertical scaling transformation we transform $T_1$ into an equilateral triangle $T_2$; the ratio of the vertical transformation equals the ratio between the $T_2$ to the $T_1$ heights; we memorise this ratio for the reverse transformation at the end of the procedure.

4. The Steiner ellipse of the equilateral triangle $T_2$ is its incircle. We are almost done; we just have to proceed to the inverse transformations; getting back from $T_2$ to $T_1$ first implies transforming the incircle of $T_2$ into an ellipse with its vertical axis scaled by the inverse ratio memorised in step 3.

5. The second inverse transformation by the shear angle is easy with the passage from $T_1$ to $T_0$, but it would be more difficult for transforming the ellipse into the sheared ellipse. We have already defined the \texttt{\Sellipse} and the \texttt{\Xellipse} macros that may take care of the ellipse shear transformation; we already memorised the shear angle in step 2, therefore the whole procedure, except for putting back the triangle, is almost done.

6. Eventually we perform the last shifting and rotating transformation and the whole construction is completed.

The new macro Steiner ellipse has therefore the following syntax:

\begin{verbatim}
\SteinerEllipse(\star)(\langle P1\rangle)(\langle P2\rangle)(\langle P3\rangle)[\langle diameter\rangle]
\end{verbatim}

where $\langle P1\rangle$, $\langle P2\rangle$, $\langle P3\rangle$ are the vertices of the triangle; $\langle \star \rangle$ is an optional asterisk; without it the maro draws only the final result, that contains only the given triangle and its Steiner ellipse; on the opposite, if the asterisk is used the whole
construction from $T_0$ to its Steiner ellipse is drawn; the labelling of points is done with little dots of the default $\langle$ diameter $\rangle$ or a specified value; by default it is a 1 pt diameter, but sometimes it would be better to use a slightly larger value (remembering that 1 mm — about three points — is already too much). Please refer to the documentation file euclideangeometry-man.pdf for usage examples and suggestions.

\begin{verbatim}
\NewDocumentCommand\SteinerEllipse{s d() d() d() O{1}}{
\bgroup
\IfBooleanTF{#1}{}{\put(#2)}{
\CopyVect0,0to\Pu
\SubVect#2from#3to\Pd
\SubVect#2from#4to\Pt
\ModAndAngleOfVect\Pd to\M and\Rot
\Mul Vect\Pd by-\Rot:1 to\Pd \Mul Vect\Pt by-\Rot:1 to\Pt
\IfBooleanTF{#1}{}{\rotatebox{\Rot}}{
\CopyVect0,0to\Pd}
\Polyline(\Pu)(\Pd)(\Pt)
\edef\B{\fpeval{\M/2}}\edef\H{\fpeval{\B*tand(60)}}
\IfBooleanTF{#1}{}{\Pbox(\B,\H)[t]{P_1}}{\Pbox(\B,\H)[b]{P_2}}{\Pbox(\B,\H)[r]{P_3}}
\polygon(\Pu)(\Pd)(\Pt)
\edef\R{\fpeval{\B*tand(30)}}
\IfBooleanTF{#1}{}{\Pbox(\B,\R)[b]{C}}{}%
\GetCoord(\Pt)\Xt\Yt\edef\VS{\fpeval{\Yt/\H}}
\IfBooleanTF{#1}{}{\Polyline(\Pu)(\B,\Yt)(\Pd)}{\Polyl ine(\Pu)(\B,\Yt)(\Pd)}
\edef\Ce{\fpeval{\B*\VS}}
\IfBooleanTF{#1}{}{\Pbox(\B,\Ce)[l]{C_i}}{}
\VectorArc(\B,0)(\B,15){-\Rot:1}{\Pbox(\B,0)[b]{B}}
\edef\a{\R}\edef\b{\Ce}
\CopyVect\fpeval{\B+\Ce*tand(\Alfa)} to\CI
\XSellisse(\CI){-\Alfa}{\R}{\Ce}
\}\
\IfBooleanTF{#1}{}{\Dotline(\B,\Yt)(\B,0){2}[1.5]}{\Dotline(\B,\Yt)(\B,0){2}[1.5]}{\Dotline(\B,\Yt)(\B,0){2}[1.5]}
\edef\a{\R}\edef\b{\Ce}
\CopyVect\fpeval{\B+\Ce*tand(\Alfa)} to\CI
\XSellisse(\CI){-\Alfa}{\R}{\Ce}
\}\
\let\EllisseSteiner\SteinerEllipse
\end{verbatim}

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1.7.3 The ellipse that is internally tangent to a triangle while one of its foci is prescribed

We now are going to tackle another problem. As we said before, any triangle has an infinite set of internally tangent circles, unless some further constraint is specified.

Another problem of this kind is the determination and geometrical construction of an internally tangent ellipse when one focus is specified; of course since the whole ellipse is totally internal to the triangle, we assume that the user has already verified that the coordinates of the focus fall inside the triangle. We are not going to check this feature in place of the user; after all, if the user draws the triangle within a picture image, together with the chosen focus, is suffices a glance to verify that such focus lays within the triangle perimeter.

The geometrical construction is quite complicated, but it is described in a paper by Estevão V. Candia on *TUGboat* 2019 40(3); it consists of the following steps.

1. Suppose you have specified a triangle by means of its three vertices, and a point inside it to play the role of a focus; it is necessary to find the other focus and the main axis length in order to have a full description of the ellipse.
2. To do so, it is necessary to find the focus three symmetrical points with respect to the three sides.
3. The center of the three point circle through these symmetrical points is the second focus.
4. The lines that join the second focus to the three symmetrical points of the first focus, intersect the triangle sides in three points that result to be the tangency points of the ellipse to the triangle.
5. Chosen one of these tangency points and computing the sum of its distances from both foci, the total length of the ellipsis main axis is found.
6. Knowing both foci, the total inter focal distance is found, therefore equation (1) allows to find the other axis length.
7. The inclination of the focal segment gives us the the rotation to which the ellipse is subject, and the middle point of such segment gives the ellipse center.
8. At this point we have all the necessary elements to draw the ellipse.

We need another little macro to find the symmetrical points; if the focus $F$ and its symmetrical point $P$ with respect to a side/segment, the intersection of such segment $F-P$ with the side is the segment middle point $M$; from this property we derive the formula $P = 2M - F$. Now $M$ is also the intersection of the line passing through $F$ and perpendicular to the side. Therefore it is particularly simple to compute, but its better to have available a macro that does the whole work; here it is, but it assumes the the center of symmetry is already known:

338 \def\SymmetricalPointOf#1respect#2to#3{\ScaleVect#2by2to\Segm\SubVect#1from\Segm to#3\ignorespaces}

20
And its syntax is the following:

\SymmetricalPointOf(focus) respect(symmetry center)
to(symmetrical point)

where the argument names are self explanatory.

The overall macro that executes all the passages described in the above enumeration follows; the reader can easily recognize the various steps, since the names of the macros are self explanatory; the $S_i$ point names are the symmetrical ones to the first focus $F$; the $M_i$ points are the centers of symmetry; the $F'$ point is the second focus; the $T_i$ points are the tangency points. The macro \EllipseWithFocus has the following syntax:

\EllipseWithFocus\{\ast\}((P_1))(\langle P_2 \rangle)(\langle P_3 \rangle)(\langle focus \rangle)

where $\langle P_1 \rangle$, $\langle P_2 \rangle$, $\langle P_3 \rangle$ are the triangle vertices and $\langle focus \rangle$ contains the first focus coordinates; the optional asterisk, as usual, selects the construction steps versus the final result: no asterisk, no construction steps.

341 \NewDocumentCommand\EllipseWithFocus{s d() d() d() d()}{\bgroup
342 \CopyVect#2to\Pu
343 \CopyVect#3to\Pd
344 \CopyVect#4to\Pt
345 \CopyVect#5to\F
346 \polygon(\Pu)(\Pd)(\Pt)
347 \Pbox(\Pu)[r]{P_1}[1.5pt]\Pbox(\Pd)[t]{P_2}[1.5pt]
348 \Pbox(\Pt)[b]{P_3}[1.5pt]\Pbox(\F)[b]{F}[1.5pt]
349 \SegmentArg(\Pu)(\Pt)to\At
350 \SegmentArg(\Pu)(\Pd)to\Ad
351 \SegmentArg(\Pd)(\Pt)to\Au
352 \IntersectionOfLines(\Pu)(\At:1)and(\F)(\fpeval{\At+90}:1)to\Mt
353 \IntersectionOfLines(\Pd)(\Ad:1)and(\F)(\fpeval{\Ad+90}:1)to\Md
354 \IntersectionOfLines(\Pt)(\Au:1)and(\F)(\fpeval{\Au+90}:1)to\Mu
355 \IfBooleanTF{#1}{\Pbox(\Mt)[br]{M_3}[1.5pt]}{}
356 \IfBooleanTF{#1}{\Pbox(\Md)[t]{M_2}[1.5pt]}{}
357 \IfBooleanTF{#1}{\Pbox(\Mu)[b]{M_1}[1.5pt]}{}
358 \SymmetricalPointOf(F respect\Mu to\Su
359 \IfBooleanTF{#1}{\Pbox(\Su)[l]{S_1}[1.5pt]}{}
360 \SymmetricalPointOf(F respect \Md to\Sd
361 \IfBooleanTF{#1}{\Pbox(\Sd)[t]{S_2}[1.5pt]}{}
362 \SymmetricalPointOf(F respect \Mt to\St
363 \IfBooleanTF{#1}{\Pbox(\St)[r]{S_3}[1.5pt]}{}
364 \IfBooleanTF{#1}{\ThreePointCircle*(\Su)(\Sd)(\St)}%
365 \IfBooleanTF{#1}{\ThreePointCircle(\Su)(\Sd)(\St)}%
366 \CopyVectC to\Fp \Pbox(\Fp)[l]{F'}[1.5pt]
367 \IfBooleanTF{#1}{\%}
368 \Dotline(\F)(\St)[2][1.5pt]
369 \Dotline(\F)(\Sd)[2][1.5pt]
370 \Dotline(\F)(\Su)[2][1.5pt]
371 \IntersectionOfSegments(\Pu)(\Pt)and(\Fp)(\St)to\Tt

21
2 Comments on this package

In general we found very comfortable to draw ellipses and to define macros to draw not only such shapes or filled elliptical areas, but also to create “legends” with coloured backgrounds and borders; such applications found their way in other works. But here we dealt with other geometrical problems. The accompanying document euclideangeometry-man.pdf describes much clearly with examples what you can do with the macros described in this package. In facts, this file just describes the package macros, and it gives some ideas on how to extend the ability of curve2e to draw geometrical diagrams. The users who would like to modify or to add some functionalities are invited to do so; I will certainly acknowledge their contributions and even add their names to the list of authors.

As long as I can, I enjoy playing with \LaTeX and its wonderful facilities; but, taking into consideration my age, I would invite the users to consider the possibility of assuming the maintenance of this package.

Aknowledgements

I am very grateful to Enrico Gregorio who let me know the several glitches I made in my first version; besides being a real \LaTeX wizard, he is a wise person and suggested me several things that was important to change, because they could offer risks of confusion with other packages.